FIRST STAGE II

Volumetric Analysis

The Third Lecture

Lecture Objective

- **Weak Acids & weak Bases**
- **Ionisation constant of weak Acids & weak Bases**
- **Weak acids pH equation**
- **Weak bases pH equation**
- **The relationship between ph, pOH, K_a, and K_b**
- **Examples**

K_a and K_b

Weak acids

Weak bases

pH, pOH, K_a, and K_b

Examples

Weak Acids & weak Bases

Weak Acids & weak Bases are **partially** ionized such as of thire:

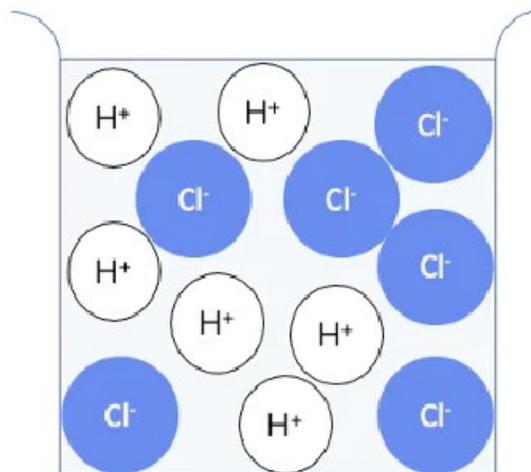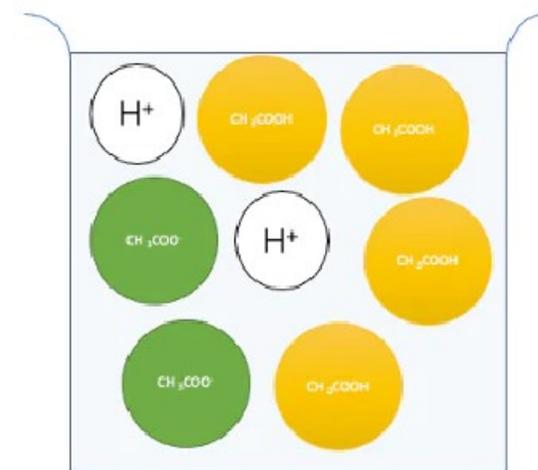| Weak acids		Weak bases	
Acetic acid	CH_3COOH	Ammonia	NH_3
Carbonic acid	H_2CO_3	Diethylamine	$(CH_3CH_2)_2NH$
Formic acid	$CHOOH$	Methylamine	CH_3NH_2
Hydrocyanic acid	HCN	Sodium bicarbonate	$NaHCO_3$
Hydrofluoric acid	HF		
Phosphoric acid	H_3PO_4		

Weak Acids & weak Bases

By contrast from strong acid & bases, weak acids and bases ionize only partially, and the ionization reaction is reversible. Thus, weak acid and base solutions contain multiple charged and uncharged species in dynamic equilibrium

Hydrochloric acid fully dissociates in water and so is a **strong acid**

Acetic acid only partially dissociates in water and so is a **weak acid**
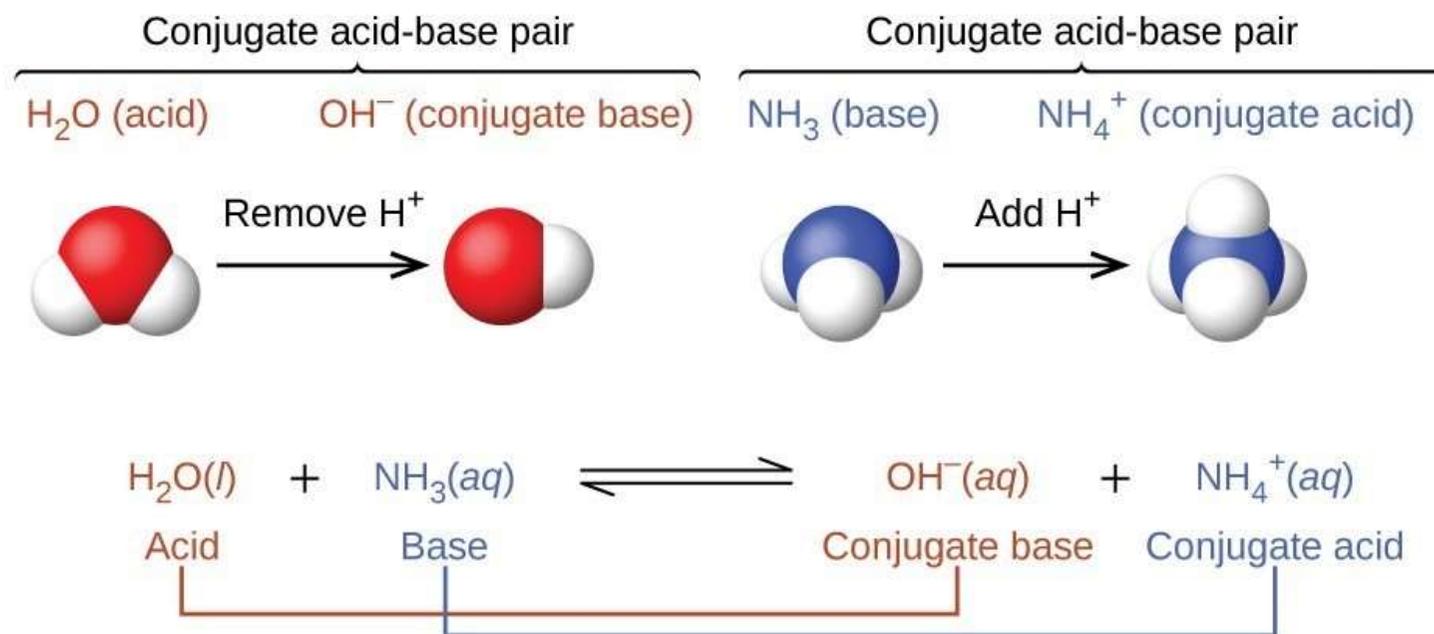
Weak Acids & weak Bases

In this connection, you probably realize that conjugate acids of weak bases are weak acids and conjugate bases of weak acids are weak bases.

K$_a$ and K$_b$

K$_a$ is an acid dissociation constant (also known as acidity constant, or acid-ionization constant.

K$_a$ is a quantitative measure of the strength of an acid in solution. It is the equilibrium constant for a chemical reaction.

$$HA + H_2O \rightleftharpoons H_3O^+ + A^-$$

$$K_a = \frac{[H_3O^+].[A^-]}{[AH]}$$ very small of water is ionised, **H$_2$O is**

constant

K_a and K_b

K_b is an base dissociation constant (also known as basicity constant, or base-ionization constant.

K_b is a quantitative measure of the strength of an base in solution. It is the equilibrium constant for a chemical reaction.

$$B + H_2O \rightleftharpoons HB^+ + OH^-$$

$$K_b = \frac{[HB^+].[OH^-]}{[B]}$$ very small of water is ionised, **H_2O is constant**

Weak acids , pH equation

$$CH_3COOH \rightleftharpoons H^+ + CH_3COO^-$$

$$K_a = \frac{[H^+].[CH_3COO^-]}{[CH_3COOH]} \quad ....(1)$$

From above equation, $[H^+] = [CH_3COO^-]$

$$K_a = \frac{[H^+]^2}{[CH_3COOH]} \quad ....(2)$$

And $[CH_3COOH] = Ca$

$$K_a = \frac{[H^+]^2}{[C_a]} \quad ....(3)$$

Weak acids , pH equation

$$K_a = \frac{[H^+]^2}{[C_a]} \quad ....(3)$$

$$[H^+]^2 = K_a \cdot [C_a] \quad ......(4)$$

$$[H^+] = K_a \cdot [C_a]^{1/2} \quad ......(5)$$

Taking loge to both sides:

$$\mp \log[H^+] = \mp \frac{1}{2}\log K_a \mp \frac{1}{2}\log[C_a]$$

$$pH = \frac{1}{2}\ pK_a - \frac{1}{2}\log C_a$$

Weak base , pOH equation

$$NH_4OH + H_2O \rightleftharpoons NH_4^+ + OH^-$$

$$K_b = \frac{[NH_4^+].[HO^-]}{[NH_4OH]} \quad ....(1)$$

From above equation, $[OH^-] = [NH_4^+]$

$$K_b = \frac{[OH^-]^2}{[NH_4OH]} \quad ....(2)$$

And $[[NH_4OH]] = C_b$

$$K_b = \frac{[OH^-]^2}{[C_b]} \quad ....(3)$$

Weak Acids & weak Bases

K_a and K_b

Weak acids

Weak bases

pH, pOH, K_a, and K_b

Examples

Weak base , pOH equation

$$K_b = \frac{[OH^-]^2}{[C_b]} \quad ....(3)$$

$$[OH^-]^2 = K_b \cdot [C_b] \quad ......(4)$$

$$[OH^-] = K_b \cdot [C_b]^{1/2} \quad ......(5)$$

Taking loge to both sides:

$$\mp \log [OH^-] = \mp \frac{1}{2} \log K_b \mp \frac{1}{2} \log[C_b]$$

$$pOH = \frac{1}{2} \ pK_b - \frac{1}{2} \log C_b$$

K_a and K_b

Weak acids

Weak bases

pH, pOH, K_a, and K_b

Examples

The Relationship pH, pOH, K_a, K_b and K_w

$$NH_4^+ + H_2O \rightleftharpoons NH_3 + H_3O^+ \qquad K_a = 5.6 \times 10^{-10}$$

$$NH_3 + H_2O \rightleftharpoons NH_4^+ + OH^- \qquad K_b = 1.8 \times 10^{-5}$$

$$H_2O + H_2O \rightleftharpoons H_3O^+ + OH^- \qquad K_w = 1.01 \times 10^{-14}$$

$$K_a \times K_b = K_w$$

$$(5.6 \times 10^{-10}) \cdot (1.8 \times 10^{-5}) = 1.01 \times 10^{-14}$$

$$K_a = \frac{[NH_3] \cdot [H_3O^+]}{[NH_4^+]} \times K_b = \frac{[NH_4^+] \cdot [HO^-]}{[NH_3]} = K_W$$

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Weak Acids & weak Bases

K_a and K_b

Weak acids

Weak bases

pH, pOH, K_a, and K_b

Examples

The Relationship pH, pOH, K_a, K_b and K_w

$$H_3O^+ \times OH^- = K_w = 1.01 \times 10^{-14} \quad \text{log to both side}$$

$$\log([H_3O^+] \times [OH^-]) = \log K_w =$$

$$\text{Log}[H_3O^+] \pm \log[OH^-] = \log 1.01 \times 10^{-14}$$

$$pH + pOH = 14$$

Weak Acids & weak Bases
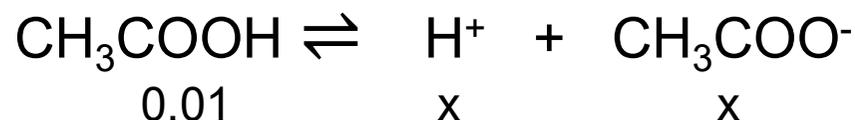
K_a and K_b

Weak acids

Weak bases

ph, pOH, K_a, and K_b

Examples

Examples

Ex. Calculate the pH of 0.01M CH_3COOH, where it's the ionization constant of acid = 1.85×10^{-5} at 25℃

Solution

$$CH_3COOH \rightleftharpoons H^+ + CH_3COO^-$$

$$\quad\quad 0.01 \quad\quad\quad\quad x \quad\quad\quad\quad x$$

$$K_a = \frac{[H^+].[CH_3COO^-]}{[CH_3COOH]}$$

$$K_a = \frac{[H^+]^2}{[C_a]}$$

$$[H^+] = K_a .[C_a]^{1/2}$$

$$\mp \log[H^+] = \mp \frac{1}{2}\log K_a \mp \frac{1}{2}\log[C_a]$$

pH = ½ pK_a – ½ $logC_a$

pH = ½ 4.74 – ½ $log10^{-2}$

pH = 2.37+ 1   **pH= 3.37**

pKa = -log Ka
    = - log 1.85×10^{-5}
    = -(5+0.026)
    = -(-4.74) === 4.74

Examples

Ex. Calculate the pH of 0.01M NH_4OH, where it's the ionization constant of base = 1.85×10^{-5} at 25℃

Solution

$$NH_4OH + H_2O \rightleftharpoons NH_4^+ + OH^-$$
$$0.01 \qquad\qquad x \qquad\qquad x$$
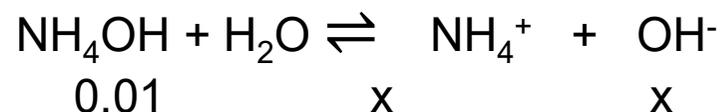
$$K_b = \frac{[NH_4^+].[HO^-]}{[NH_4OH]}$$

$$K_b = \frac{[OH^-]^2}{[C_b]}$$

$$[OH^-] = K_b.[C_b]^{1/2}$$
$$\mp\log[OH^-] = \mp\frac{1}{2}\log K_b \mp \frac{1}{2}\log[C_b]$$
pOH = ½ pK_b – ½ logC_b

pOH = ½ 4.74 – ½ log10^{-2}
pOH = 2.37+ 1
pOH= 3.37   pH = 14 – 3.37 = 10.63

$$pK_b = -\log K_b$$
$$= -\log 1.85 \times 10^{-5}$$
$$= -(5+0.026)$$
$$= -(-4.74) === 4.74$$

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Examples

Ex. K_b methylamine 3.7×10^{-4} calculate the K_a value of methylammonium ion ?

Solution

$$CH_3NH_2 + H_2O \rightleftharpoons CH_3NH_3^+ + OH^-$$

$$CH_3NH_3^+ + H_2O \rightleftharpoons CH_3NH_2 + H_3O^+$$

$$K_a \times K_b = K_w$$

$$K_a \times 3.7 \times 10^{-4} = 1.01 \times 10^{-14}$$

$$K_a = 2.7 \times 10^{-11}$$

$K_a \times K_b = K_w$ x (log)

$\log (K_a \times K_b) = \log K_w$

$-\log K_a \mp \log K_b = -\log K_w$

$-\log 2.7 \times 10^{-11} \mp \log K_b = -\log K_w$

$10.57 + pK_b = 14$

$pK_b = 3.43$

pKa = -log Ka
   = - log 2.7×10^{-11}
   = -(-11+0.43)
   = -(-10.57) === 10.57

REVIEW

- **How to weak acids and bases un ionization?**
- **Equilibrium reaction of weak Acid & base**
- **Conjugate acids bases?**
- **K_a and K_b**
- **Derive pH equation**
- **pH calculation of weak acids and bases equation**
- **The relationship between pH, pOH, K_a, and K_b**
- **Examples**

Home Work

1. **Calculate the pH and pOH of the following acidic solutions?**
   (a) 0.02 M HCN
   (b) 0.8 g of HCN dissolve to 100 ml water $K_{a\ HCN} = 6.2 \times 10^{-10}$

2. **Calculate the pH and pOH of the following basic solutions?**
   (a) 0.075 M NH_3
   (b) 1 mL of 0.1M of NH_3 add to 100 ml water $K_{b\ NH_3} = 1.8 \times 10^{-5}$